AQA

Please write clearly in block capitals.

Centre number | | | | | | Candidate number | | | | |
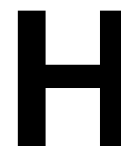
Surname

Forename(s)

Candidate signature

I declare this is my own work.

GCSE
MATHEMATICS

H

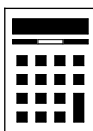Higher Tier   Paper 2 Calculator

Thursday 3 November 2022   Morning   Time allowed: 1 hour 30 minutes

Materials
For this paper you must have:
- a calculator
- mathematical instruments
- the Formulae Sheet (enclosed).

Instructions
- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross through any work you do not want to be marked.

Information
- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer book.

Advice
In all calculations, show clearly how you work out your answer.

For Examiner's Use	
Pages	Mark
2–3	
4–5	
6–7	
8–9	
10–11	
12–13	
14–15	
16–17	
18–19	
20–21	
22–23	
24	
TOTAL	

Answer **all** questions in the spaces provided.

1 2 Work out $\dfrac{4^6 - 11}{\sqrt{625} - 225}$

Circle your answer.

[1 mark]

−61.6   −20.425   204.25   3870.56

2 Work out $\left(3.1 \times 10^9\right)^2$

Circle your answer.

[1 mark]

6.2×10^{18} 6.2×10^{81} 9.61×10^{18} 9.61×10^{81}

3 The equation of a line is $y = 3x - 6$

Circle the coordinates of the y-intercept.

[1 mark]

$(0, -6)$ $(-6, 0)$ $(0, 3)$ $(3, 0)$

Do not write outside the box

4 $a \times b^4 = c$

Circle the correct expression for a.

[1 mark]

$$\frac{c}{\sqrt[4]{b}} \qquad\qquad \frac{c}{b^{-4}} \qquad\qquad \left(\frac{c}{b}\right)^4 \qquad\qquad \boxed{\frac{c}{b^4}} \ \text{①}$$

5 Written as the product of prime factors,

$$12\,600 = 2^3 \times 3^2 \times 5^2 \times 7$$

and

$$14\,112 = 2^5 \times 3^2 \times 7^2$$

Work out the highest common factor (HCF) of $12\,600$ and $14\,112$

Give your answer as an integer.

[2 marks]

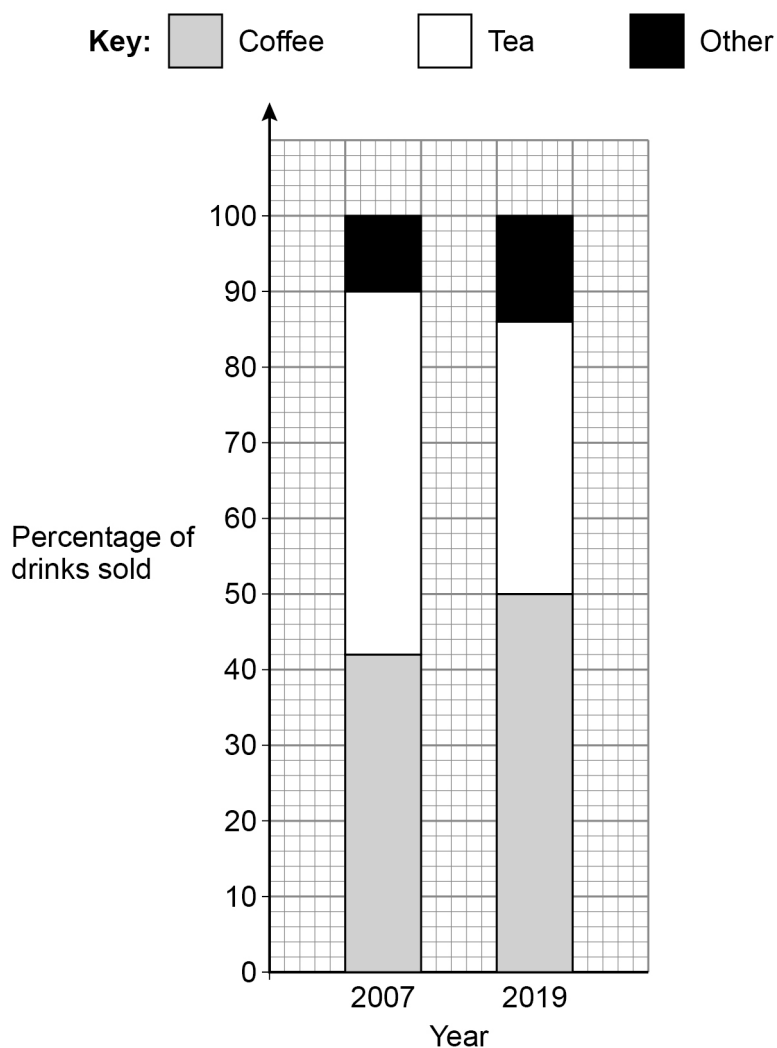HCF : $2^3 \times 3^2 \times 7 = 8 \times 9 \times 7$
 ①
$= 504$ ①

Answer 504

6

IB/M/Nov22/8300/2H

6 The composite bar chart shows information about the **percentage** of drinks sold by a café in 2007 and 2019

Key: ☐ Coffee ☐ Tea ■ Other

Percentage of drinks sold

Year

6 (a) In 2007 the café sold a total of 24 000 drinks.

How many **more** teas than coffees were sold?

[2 marks]

Tea : 90 − 42 = 48 %

Coffee : 42 %

48 − 42 = 6 %   ①

$\frac{6}{100} \times 24\,000 = 1440$

Answer _____1440_____ ①

6 (b) Were more coffees sold at the café in 2019 than in 2007 ?

Tick a box.

☐ Yes   ☐ No   ☑ Cannot tell

Give a reason for your answer.

[1 mark]

The total numbers sold in 2019 were unknown. ①

7 (a) k is a whole number between 40 and 50

The cube root of k is 3, to the nearest whole number.

Work out the **largest** possible value of k.

[2 marks]

$3.5^3 = 42.875$ ①

$k = 42$

Answer _____ 42 ①

7 (b) Fay tries to solve $x^2 = 100$

She says,

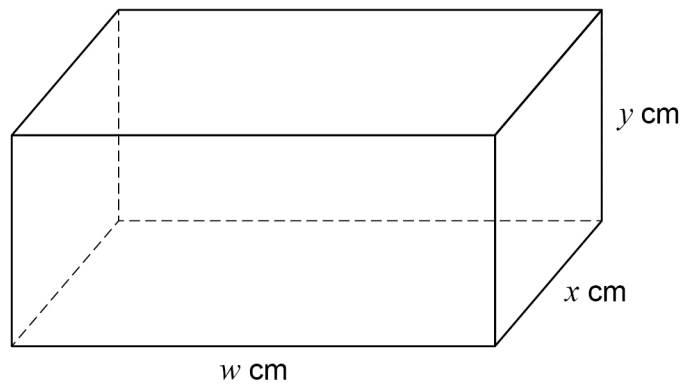"The only possible value of x is 10"

Give a reason why she is **not** correct.

[1 mark]

x could also be -10 ①

8 (a) Here is a cuboid.

w, x and y are **different** whole numbers.

The total length of **all** the edges of the cuboid is 80 cm

The volume is **greater** than 200 cm^3

Work out one possible set of values for w, x and y.

[2 marks]

$4w + 4y + 4x = 80$

$4(w + x + y) = 80$
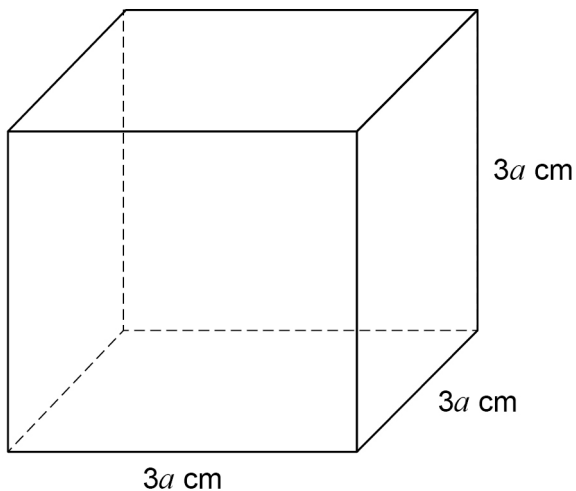
$w + x + y = 20$

$wxy > 200$

let $w = 8$, $x = 7$, $y = 5$

$8 + 7 + 5 = 20$, $8 \times 7 \times 5 = 280$

②

$w = \underline{\quad 8 \quad}$ $x = \underline{\quad 7 \quad}$ $y = \underline{\quad 5 \quad}$

Do not write outside the box

8 (b) Here is a solid cube.

$3a$ cm

$3a$ cm

$3a$ cm

$6(3a \times 3a)$

Circle the expression for the **total** surface area in cm² $6(9a^2)$

$54a^2$

[1 mark]

36a 54a 36a^2 $54a^2$ ①

9 The 47th triangular number is 1128

The 48th triangular number is 1176

Work out the 49th triangular number.

[1 mark]

$\frac{49(50)}{2} = 1225$
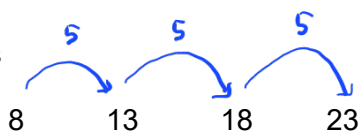
Answer   1225 ①

4

Turn over ▶

IB/M/Nov22/8300/2H

10 The nth terms of two linear sequences, A and B, are added to give the nth term of a new sequence.

The new sequence starts

$$\overset{5}{\frown} \quad \overset{5}{\frown} \quad \overset{5}{\frown}$$

8　　13　　18　　23

The nth term of sequence A is　$n + 1$

Work out the nth term of sequence B.

[4 marks]

$a = 8$, $d = 5$　①

$T_n = 8 + (n-1) 5$

$= 8 + 5n - 5$

$= 5n + 3$　①

$A + B = 5n + 3$

$n+1 + B = 5n + 3$

$B = 5n - n + 3 - 1$　①

$= 4n + 2$

Answer　$4n + 2$　①

11 A tank contains 40 litres of water.

11 (a) Water leaks out of the tank at a rate of 1.2 litres per minute.

The leak is stopped after 20 minutes.

Show that, when the leak is stopped, the tank contains 16 litres of water.

[1 mark]

Total water leaks : $1.2 \times 20 = 24$ litres

①

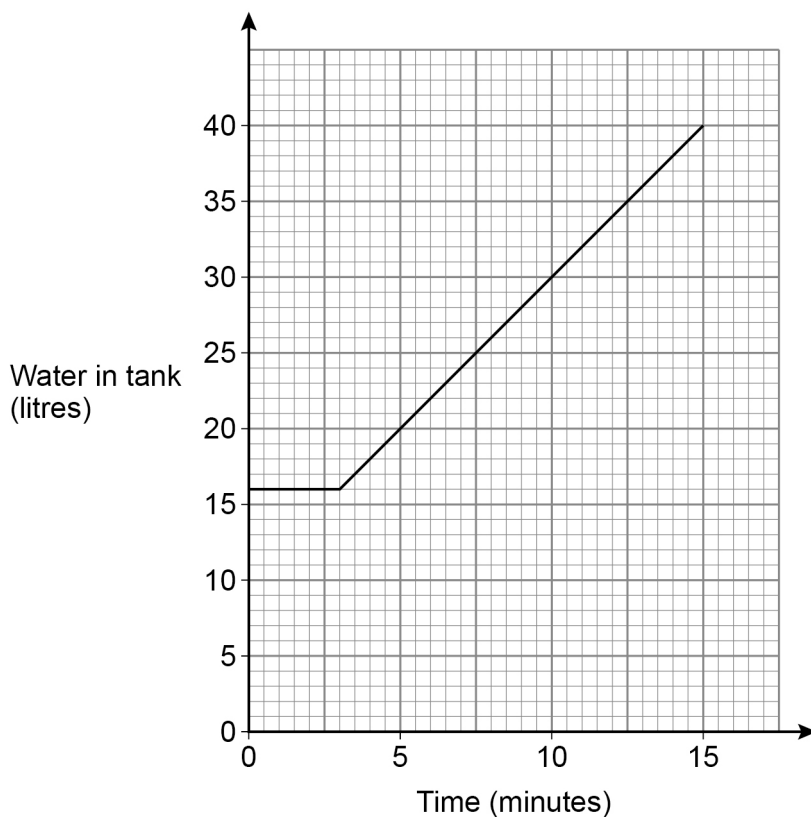$40 - 24 = 16$

Do not write outside the box

11 (b) The tank is refilled with water from a tap.

The graph shows the amount of water in the tank **after** the leak is stopped.

Complete this report by writing a number in each answer space.

[3 marks]

Report

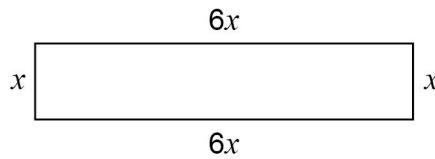_____3____ ① minutes after the leak is stopped, the tap starts to refill the tank.

The rate at which the tank refills is ____2____ litres per minute.
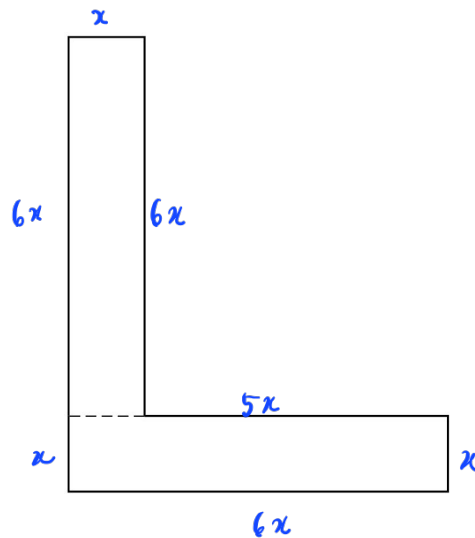

$$\frac{40-16}{15-3} = \frac{24}{12} = 2$$

① ①

8

Turn over ▶

IB/M/Nov22/8300/2H

Do not write outside the box

12 The length of this rectangle is 6 times the width.

$6x$

x ☐ x

Not drawn accurately

$6x$

Two of these rectangles are joined, with no overlap, to make this L-shape.

x

Not drawn accurately

$6x$ $6x$

$5x$

x x

$6x$

The perimeter of the L-shape is 98.8 cm

Work out the value of the perimeter of **one** of the rectangles.

[4 marks]

$6x + x + 6x + 5x + x + 6x + x = 98.8$

$26x = 98.8$

① $x = 98.8 \div 26$ ①
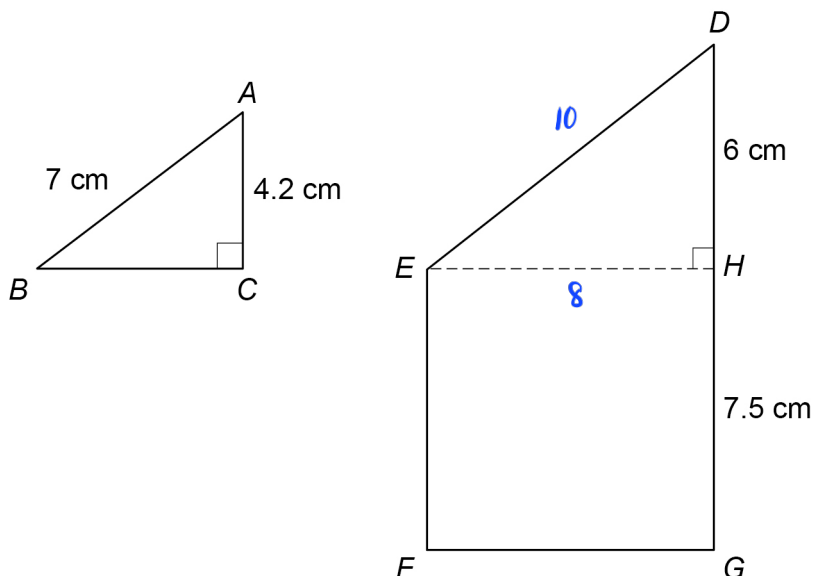
$= 3.8$

Perimeter of one rectangle : $x + x + 6x + 6x$

$= 14x = 14(3.8)$ ①

$= 53.2$ ①

Answer _____ 53.2 _____ cm

1 0

Do not write
outside the
box

13 Trapezium *DEFG* is formed by joining

triangle *DEH*

to

rectangle *EFGH*.

A

7 cm   4.2 cm

B

C

D

10

6 cm

E

8

H

7.5 cm

F

G

Not drawn
accurately

ABC is similar to *DEH*.

Work out the area of *DEFG*.

[5 marks]

$$\frac{DE}{7} = \frac{6}{4.2}$$

$$DE = \frac{6}{4.2} \times 7 = 10 \quad (1)$$

$$EH = \sqrt{10^2 - 6^2} \quad (1)$$

$$= \sqrt{64} = 8 \quad (1)$$

Area DEH $= \frac{1}{2} \times 6 \times 8 = 24$ (1)

Area EFGH $= 8 \times 7.5 = 60$

Area DEFG $= 24 + 60 = 84$

Answer _____ 84 (1) _____ cm^2

9

Turn over ▶

14 Fred bought an apartment for £137 500

He made 8% profit when he sold the apartment.

He used all of this profit to pay 40% of the deposit on a house.

The deposit was one sixth of the price of the house.

Work out the price of the house.

[4 marks]

Profit : $\frac{8}{100} \times 137\,500 = 11\,000$ ①

$11\,000 = 40\%$ of deposit

deposit $= \frac{11\,000}{0.4} = 27\,500$ ①

price of the house $= 27\,500 \times 6$ ①

$= 165\,000$ ①

Answer £ __165 000__

15 Circle the correct statement.

[1 mark]

$1\ m^2 = 100\ mm^2$ $1\ cm^2 = 100\ mm^2$ $1\ m^2 = 100\ cm^2$ $1\ km^2 = 100\ m^2$

Do not write outside the box

16 Here is a sketch of a graph.
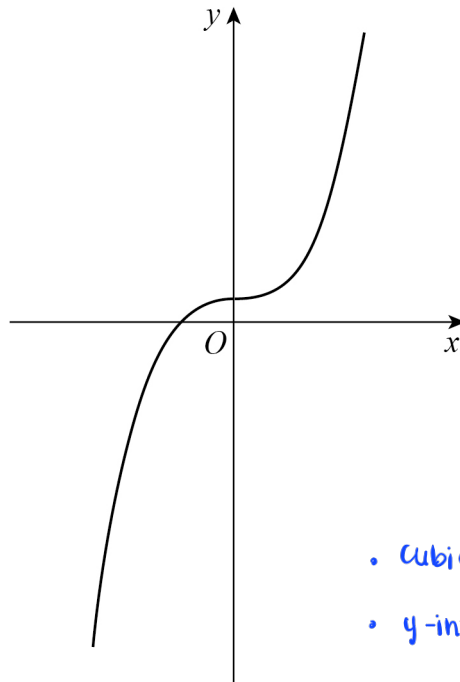
- cubic graph
- y-intercept positive value

Circle the possible equation of the graph.

[1 mark]

$y = x^2 + 1$ $\qquad$ $y = \dfrac{1}{x} + 1$ $\qquad$ $\boxed{y = x^3 + 1}$ ① $\qquad$ $y = 1 - x^2$

17 A sequence of numbers is formed by the iterative process

$$u_{n+1} = \frac{20}{u_n + 3} \qquad \text{where} \qquad u_1 = 1$$

Work out u_3

$u_2 = \dfrac{20}{4} = 5 \qquad u_3 = \dfrac{20}{8} = \dfrac{5}{2}$

Circle your answer.

[1 mark]

$\dfrac{40}{11}$ $\qquad$ $\boxed{\dfrac{5}{2}}$ ① $\qquad$ 7 $\qquad$ 5
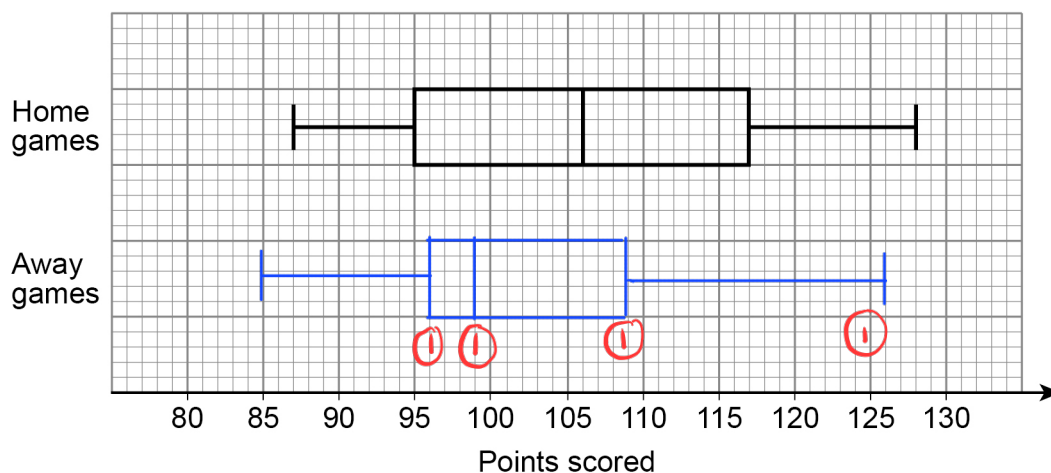
7

Turn over ▶

Do not write outside the box

18 A basketball team plays 19 home games and 19 away games.

The box plot shows information about the points the team scored in **home** games.

Home games

Away games

80 85 90 95 100 105 110 115 120 125 130

Points scored

Here are the points the team scored in the 19 **away** games.

LQ   median

85   89   93   95   ⟨96⟩   96   98   98   98   ⟨99⟩

100   103   105   107   ⟨109⟩   110   114   119   126

UQ

18 (a) On the grid, draw a box plot for the away games.

[4 marks]

Median : $\frac{19+1}{2}$ = 10th term = 99

LQ = 96

UQ = 109

Do not write outside the box

18 (b) On average, did the team score more points in home games or away games?

Use **one** statistical measure to support your decision.

[1 mark]

Home as the median is higher . ①

18 (c) Was the number of points scored more consistent in home games or away games?

Use **one** statistical measure to support your decision.

[1 mark]

Away as the interquartile range is lower. ①

19 Using the quadratic formula, or otherwise, solve $3x^2 + x - 5 = 0$

[2 marks]

$$x = \frac{-1 \pm \sqrt{1^2 - 4(3)(-5)}}{2(3)} \quad ①$$

$$= \frac{-1 \pm \sqrt{61}}{6}$$

$$= \frac{-1 - \sqrt{61}}{6} \quad \text{or} \quad \frac{-1 + \sqrt{61}}{6}$$

$$= -1.468... \quad \text{or} \quad 1.135...$$

Answer $-1.468...$ and $1.135...$ ①

8

Turn over ▶

Do not write outside the box

20 A vending machine has a different item in each section.

It sells

       7 drinks, 3 of which are juice

       5 snacks, 2 of which are fruit bars

       11 meals, 4 of which are salad.

One drink, one snack and one meal are chosen at random.

Show that the probability of getting a juice, a fruit bar and a salad is **more** than 5%

[3 marks]

$$\frac{3}{7} \times \frac{2}{5} \times \frac{4}{11} = \frac{24}{385}$$

$$= 0.0623 \times 100\%$$

$$= 6.23\%$$

Do not write outside the box

21 $f(x) = \dfrac{3x+9}{5}$ and $g(x) = 6x - 1$

21 (a)   Show that gf(2) is an integer.

[2 marks]

$$gf(x) = \frac{6(3x+9)}{5} - 1 \quad ①$$

$$= \frac{18x + 54}{5} - 1$$

$$gf(2) = \frac{18(2) + 54}{5} - 1$$

$$= \frac{36 + 54}{5} - 1$$

$$= 18 - 1 = 17 \quad ①$$

21 (b)   Show that $f^{-1}(8)$ is **not** an integer.

[2 marks]

$$\text{let } f(x) = \frac{3x+9}{5}$$

$$y = \frac{3x+9}{5}$$

$$5y = 3x + 9$$

$$5y - 9 = 3x$$

$$x = \frac{5y-9}{3}$$

$$f^{-1}(x) = \frac{5x-9}{3} \;①\; = \frac{5(8)-9}{3} = \frac{31}{3} = 10.3 \;①$$

7

Turn over ▶

22   Factorise fully $x^3 - 49x$

[2 marks]

$x(x^2 - 49)$ ①

$x(x-7)(x+7)$ ①

Answer $x(x-7)(x+7)$

23   61 students recorded how many hours they spent revising for a test.

The histogram represents the results.

Do not write outside the box
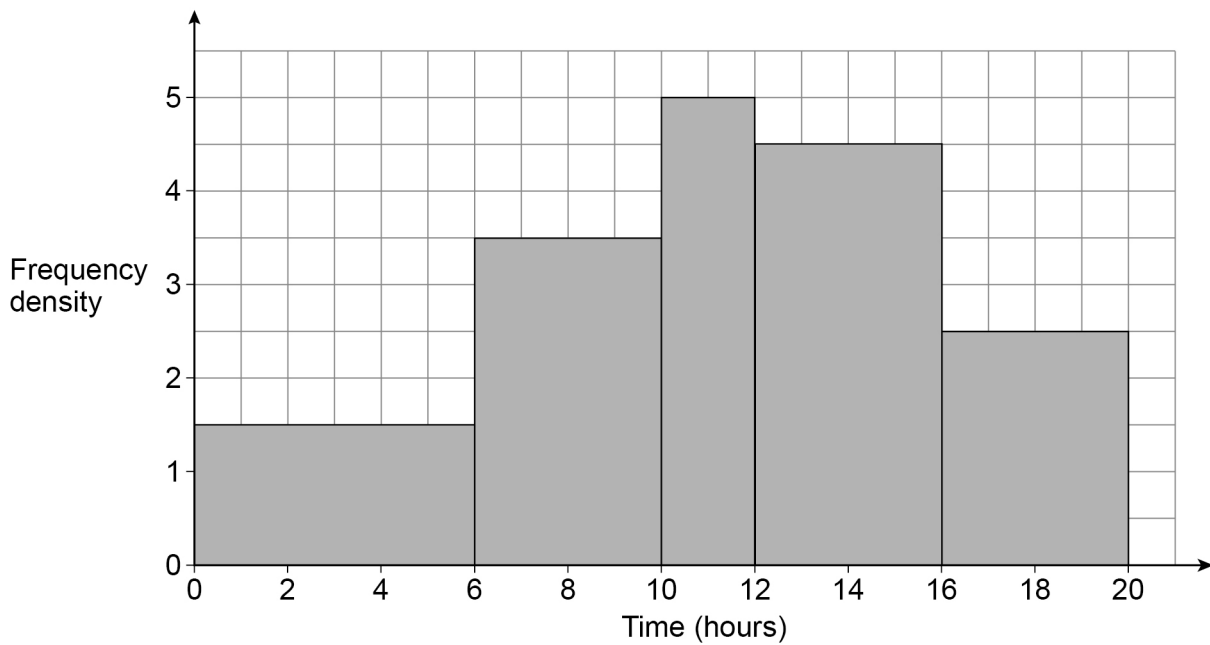
23 (a) Work out an estimate of the mean time the 61 students spent revising.

You may use the table to help you.

[4 marks]

	A	B	A × B
Time, x (hours)	**Frequency**	**Midpoint**	
$0 \leqslant x < 6$	9	3	27
$6 \leqslant x < 10$	14	8	112 ①
$10 \leqslant x < 12$	10	11	110
$12 \leqslant x < 16$	18	14	252
$16 \leqslant x < 20$	10	18	180

$6 \times 1.5 = 9$, $4 \times 3.5 = 14$, $2 \times 5 = 10$, $4 \times 4.5 = 18$, $4 \times 2.5 = 10$ ①

$$\text{mean} = \frac{27 + 112 + 110 + 252 + 180}{61}$$

$$= \frac{681}{61} \ ① = 11.16 \ ①$$

Answer _____11.16_____ hours

23 (b) Give a reason why the answer to part (a) is an estimate.

[1 mark]

The midpoints are estimates ①

7

Turn over ▶

Do not write outside the box

24 B is 60 miles from A on a bearing of 170°

Not drawn accurately

N

A × 170°

34.5   77°

60 miles

x

62.1   × B
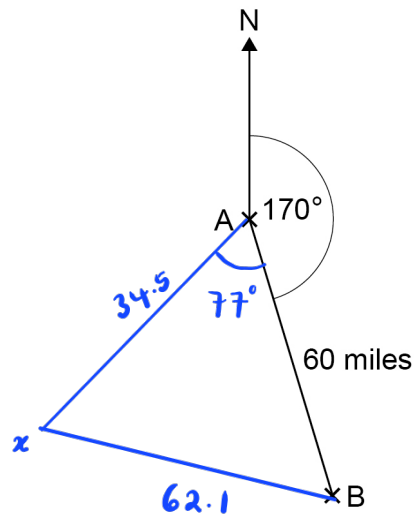
A ship sails from A on a bearing of 247°

It travels at a constant speed of 23 mph for $1\frac{1}{2}$ hours.

Is the ship now closer to B than it was when it left A?

You **must** show your working.

[5 marks]

$$247° - 170° = 77° ①$$

$$distance = 23 \times 1.5 = 34.5 ①$$

$$xB^2 = 34.5^2 + 60^2 - 2(34.5)(60)\cos 77° ①$$
$$= 3858$$

$$xB = \sqrt{3858} ①$$
$$= 62.1$$

①

No. The ship is further away.

25   Two congruent parallelograms, *PQRV* and *VRST*, are joined.

Not drawn accurately
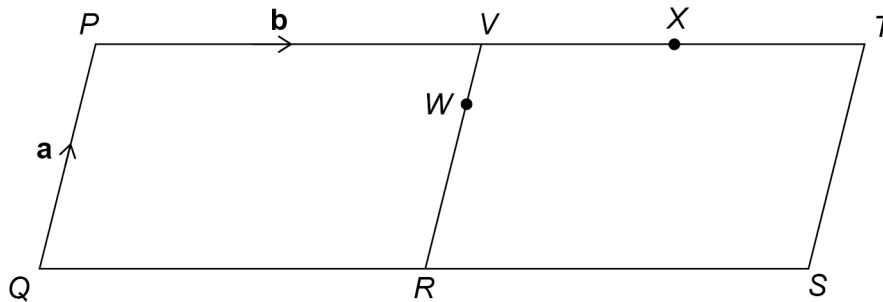
$\overrightarrow{QP} = \mathbf{a}$ $\overrightarrow{PV} = \mathbf{b}$

X is the midpoint of *VT*.

VW : *WR* = 1 : 2

Prove that *Q, W* and *X* lie on a straight line.

[3 marks]

$$\overrightarrow{QW} = \overrightarrow{QP} + \overrightarrow{PV} + \overrightarrow{VW}$$

$$= \underline{a} + \underline{b} + \frac{1}{3}(\overrightarrow{VR})$$

$$= \underline{a} + \underline{b} - \frac{1}{3}\underline{a}$$

$$= \frac{2}{3}\underline{a} + \underline{b} \quad ①$$

$$\overrightarrow{QX} = \overrightarrow{QP} + \overrightarrow{PV} + \overrightarrow{VX}$$

$$= \underline{a} + \underline{b} + \frac{1}{2}(\overrightarrow{VT})$$

$$= \underline{a} + \underline{b} + \frac{1}{2}\underline{b}$$

$$= \underline{a} + \frac{3}{2}\underline{b} \quad ①$$

$$\overrightarrow{QW} = \frac{3}{2}\left(\frac{2}{3}\underline{a} + \underline{b}\right) = \underline{a} + \frac{3}{2}\underline{b} = \overrightarrow{QX}$$

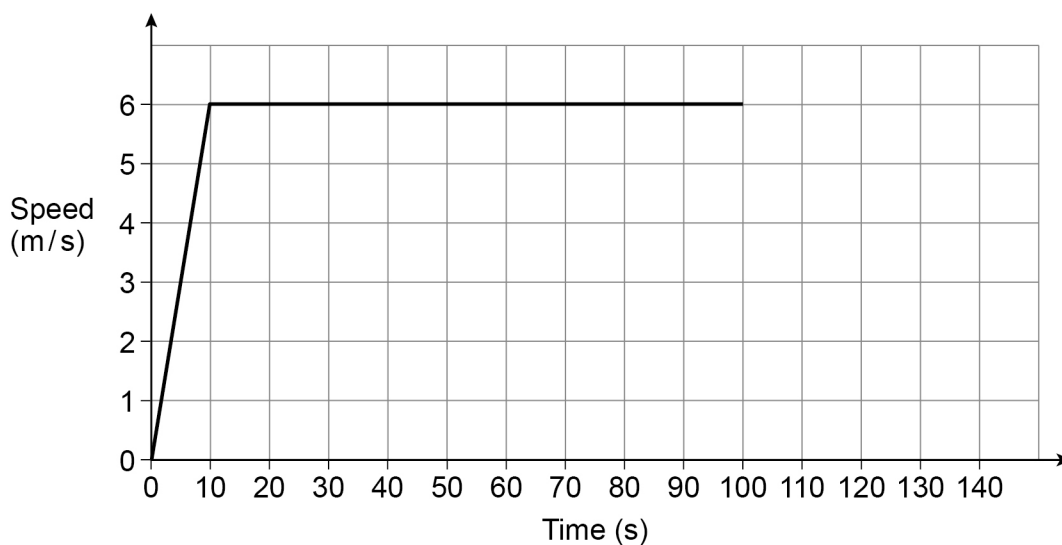$$\overrightarrow{QW} = \frac{3}{2}\overrightarrow{QX} \quad ①$$

8

Turn over ▶

26 Helena ran an 800-metre race in 140 seconds.

The speed-time graph represents the first 100 seconds of her run.

Helena ran the last 40 seconds with constant deceleration.

Work out her speed as she finished the race.

[4 marks]

$\text{distance}_1 = \frac{1}{2} \times 10 \times 6 = 30 \text{ m}$ ①

$\text{distance}_2 = 6 \times 90 = 540 \text{ m}$

$\text{distance ran} = 30 + 540 = 570 \text{ m}$

$800 - 570 = 230 \text{ m}$ balance ①

$\frac{1}{2} \times (v+6) \times 40 = 230$ ①

$v + 6 = 11.5$

$v = 5.5$ ①

Answer _____5.5_____ metres per second

Do not write outside the box

27 In a class there are

n boys

a total of 25 students.

Two of the students are chosen at random.

The probability that both students are boys is $\dfrac{7}{20}$

Work out the value of n.

[4 marks]

$$\frac{n}{25} \times \frac{n-1}{24} = \frac{7}{20}$$

$$\frac{n^2-n}{600} = \frac{7}{20}$$

$$n^2 - n = 210$$

$$n^2 - n - 210 = 0$$

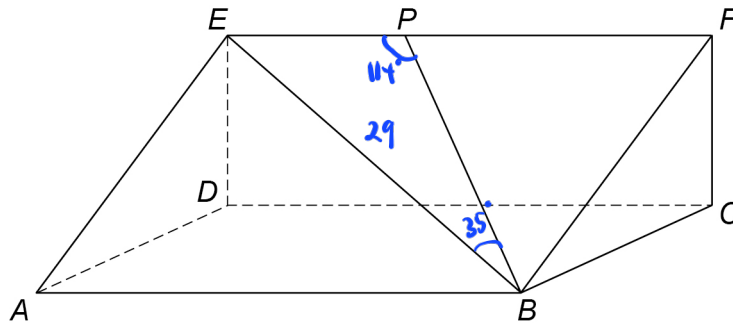$$(n-15)(n+14) = 0$$

$$n = 15 \quad \text{or} \quad n = -14$$

n should be positive, hence $n = 15$

$n = \underline{\qquad 15 \qquad}$

8

Turn over ▶

28   *ABCDEF* is a triangular prism.

P is a point on *EF*.

EB = 29 cm

Angle *EBP* = 35°

Angle *EPB* = 114°

Work out the length of *EP*.

[2 marks]

$$\frac{EP}{\sin 35°} = \frac{29}{\sin 114°} \quad ①$$

$$EP = \frac{29}{\sin 114°} \times \sin 35°$$

$$= 18.2 \quad ①$$

Answer   18.2   cm

END OF QUESTIONS

2

Do not write outside the box

There are no questions printed on this page

DO NOT WRITE ON THIS PAGE
ANSWER IN THE SPACES PROVIDED

Question number	Additional page, if required. Write the question numbers in the left-hand margin.

Do not write outside the box

Question number	Additional page, if required. Write the question numbers in the left-hand margin.

Do not write outside the box

Question number	Additional page, if required. Write the question numbers in the left-hand margin.